### Lecture #13

# **Modeling of Hydro-Electrometallurgical Processes**

Hydro-electrometallurgy involves the use of aqueous solutions to extract and recover metals via electrochemical processes. These processes are integral to industries producing high-purity metals and alloys. Modeling such processes provides insights into reaction kinetics, mass transport, and energy efficiency.

This lecture focuses on modeling hydro-electrometallurgical processes, with examples of copper electrochemical recovery and nickel electroextraction. Key modeling considerations include electrolyte composition, electrode surface reactions, and transport phenomena.

## **Copper Electrochemical Recovery**

Copper recovery from industrial waste streams or leach solutions is a critical process for sustainable resource management. The electrochemical reactions occur at the cathode and anode, as shown below:

- Cathode reaction:  $Cu^{2+} + 2e^{-} \rightarrow Cu(s)$
- Anode reaction:  $2H_2O \rightarrow O_2 + 4H^+ + 4e^-$

Key equations for modeling copper recovery include:

1. Nernst Equation: Determines the equilibrium potential as a function of Cu<sup>2+</sup> concentration.

$$E = E^{0} - (RT/2F) \ln(C_{C}u^{2+})$$

2. Butler-Volmer Equation: Models current density (i) based on overpotential  $(\eta)$ :

$$i = i_0 \left[ \exp(\alpha F \eta / RT) - \exp(-\beta F \eta / RT) \right]$$

Mass transport is modeled using Fick's law for diffusion and convective contributions in stirred systems:

$$\partial C/\partial t = D \nabla^2 C - (v \cdot \nabla C)$$

#### **Nickel Electroextraction**

Nickel electroextraction involves recovering nickel from aqueous solutions, typically containing nickel sulfate (NiSO<sub>4</sub>). The electrochemical reactions are:

- Cathode reaction:  $Ni^{2+} + 2e^{-} \rightarrow Ni(s)$
- Anode reaction:  $H_2O \rightarrow \frac{1}{2}O_2 + 2H^+ + 2e^-$

Key factors for modeling include:

1. Electrodeposition rate, modeled as:

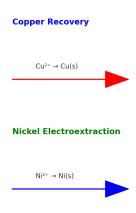
$$m = (M_i / zF) \int i dt$$

where m is the mass of deposited metal, M\_i is the molar mass, z is the number of electrons, and F is Faraday's constant.

2. Mass transport, affected by diffusion and migration in the electrolyte.

An additional consideration is the effect of impurities, which can alter electrode kinetics and deposition morphology.

# **Illustration: Hydro-Electrometallurgical Processes**



The schematic illustrates the electrochemical reactions involved in copper recovery and nickel electroextraction. These processes are characterized by electrode reactions and transport phenomena in the electrolyte.

## **Summary**

Modeling hydro-electrometallurgical processes provides valuable insights into the reaction kinetics, mass transport, and energy efficiency of metal recovery systems. Copper electrochemical recovery focuses on reducing Cu<sup>2+</sup> to Cu, while nickel electroextraction involves reducing Ni<sup>2+</sup> to Ni. Understanding these processes is critical for optimizing industrial operations and improving sustainability.